



# Recursive Structures and Processes

# Announcements

- **LS15: Recursive Structures** due tomorrow and 11:59pm
- **EX07: Linked List Utility Functions** released today

First, a review of recursion...

# Review: Recursive function checklist:

## Base case:

- ❑ Does the function have a clear base case?
  - ❑ Ensure the base case returns a result directly (without calling the function again).
- ❑ Will the base case *always* be reached?

## Recursive case:

- ❑ Does the function have a recursive case that *progresses toward the base case*?
  - ❑ Does the recursive call have the right arguments? The function should call itself on a simpler or smaller version of the problem.
- ❑ Have you tested your function with multiple cases, including edge cases?

# Review: Stack Overflow and Recursion Errors

When a programmer writes a function that calls itself indefinitely (*infinitely*), the **function call stack** will *overflow*...

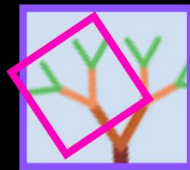
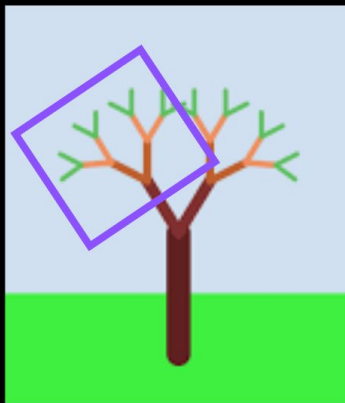
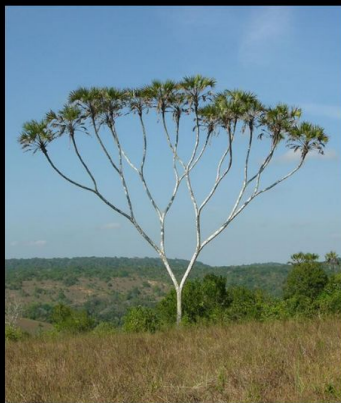
This leads to a **Stack Overflow Or Recursion Error**:

```
RecursionError: maximum recursion depth exceeded while  
calling a Python object
```

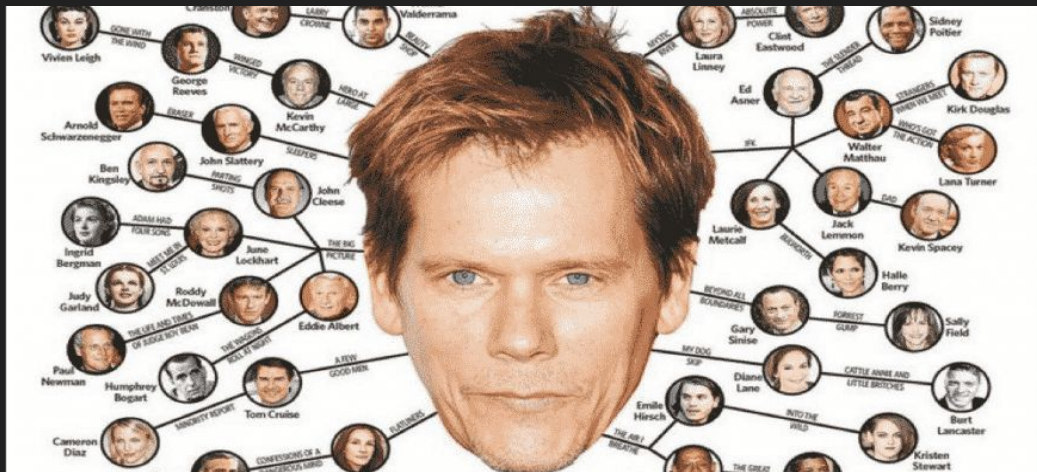
# Recursion: defining an operation/object in terms of itself

A real-world phenomenon! Examples:

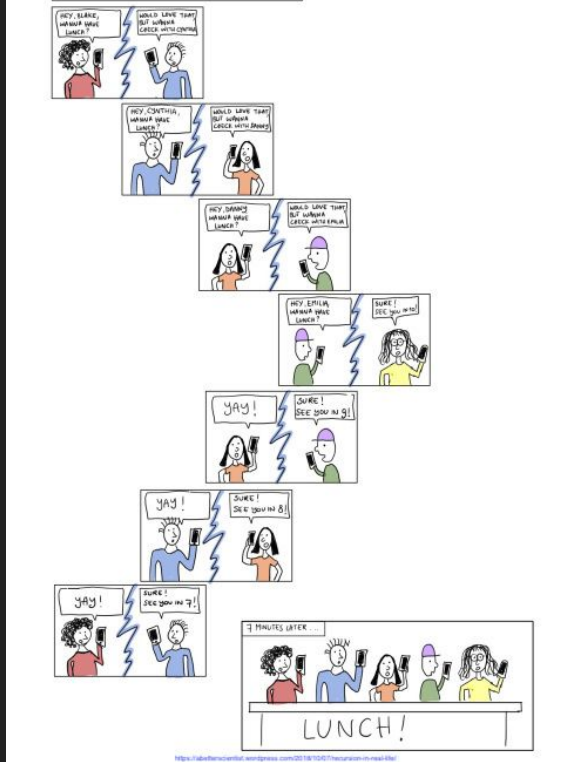
- **You** have **parents**, who have **parents**, who have **parents**, who have **parents**, who...  
... were **early humans**
- A **tree** has **branches**, which have **branches**, which have **branches**, which...  
... have **leaves**



# Different recursive structures for different purposes



Six degrees of Kevin Bacon  
graph/network



Coordinating plans with  
individual phone calls  
linked list

# Anatomy of a Singly-Linked List

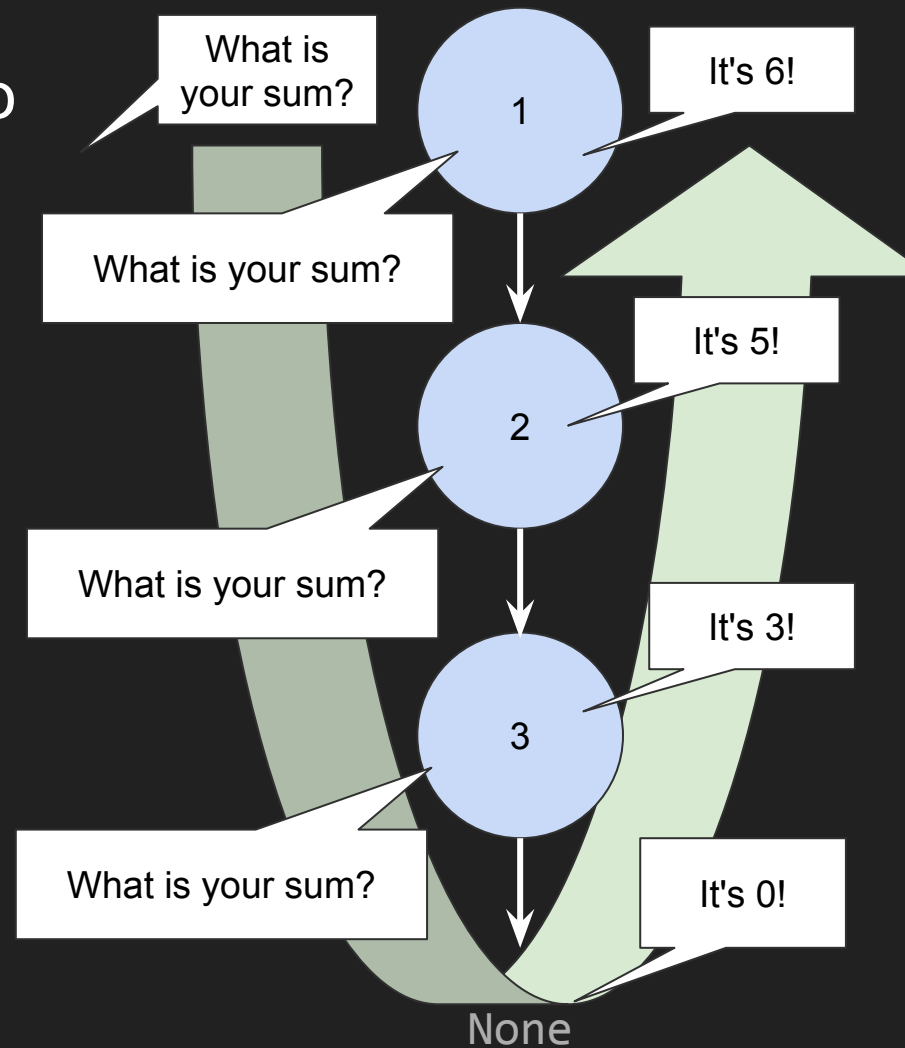


# Memory diagram

```
1  from __future__ import annotations
2
3  class Node:
4      value: int
5      next: Node | None
6
7      def __init__(self, val: int, next: Node | None):
8          self.value = val
9          self.next = next
10
11  # Note: There are no errors!
12  two: Node = Node(2, None)
13  one: Node = Node(1, two)
14  # We'll extend this diagram shortly, leave room
```

# A Recursive `sum` Algorithm Demo

1. When you are asked, "what is your sum?"
2. Ask the **next** Node, "what is your sum?"  
Wait patiently for an answer!
3. Once the answer is returned back to you, add **your value to it**, then turn to the person who asked you and give them this answer.



In your exercises folder, create a folder named `ex07`. In `ex07`, create a file named `linked_list.py`. Then, copy the following code into `linked_list.py`

```
1 from __future__ import annotations
2
3
4 class Node:
5     """Node in a singly-linked list recursive structure."""
6
7     value: int
8     next: Node | None
9
10    def __init__(self, value: int, next: Node | None):
11        self.value = value
12        self.next = next
13
14
15 two: Node = Node(2, None)
16 one: Node = Node(1, two)
```

# Let's write a recursive function called `sum`!

```
1  from __future__ import annotations
2
3  class Node:
4      value: int
5      next: Node | None
6
7      def __init__(self, val: int, next: Node | None):
8          self.value = val
9          self.next = next
10
11  # Note: There are no errors!
12  two: Node = Node(2, None)
13  one: Node = Node(1, two)
14  # We'll extend this diagram shortly, leave room
```

Write a function called `sum` that adds up the `values` of all `Nodes` in the linked list.

# For reference: recursive function checklist:

## Base case:

- ❑ Does the function have a clear base case?
  - ❑ Ensure the base case returns a result directly (without calling the function again).
- ❑ Will the base case *always* be reached?

## Recursive case:

- ❑ Does the function have a recursive case that *progresses toward the base case*?
  - ❑ Does the recursive call have the right arguments? The function should call itself on a simpler or smaller version of the problem.
- ❑ Have you tested your function with multiple cases, including edge cases?

# Diagramming the `sum` function call

```
1  from __future__ import annotations
2
3  class Node:
4      value: int
5      next: Node | None
6
7      def __init__(self, value: int, next: Node | None):
8          self.value = value
9          self.next = next
10
11
12  two: Node = Node(2, None)
13  one: Node = Node(1, two)
14
15  def sum(head: Node | None) -> int:
16      if head is None:
17          return 0
18      else:
19          return head.value + sum(head.next)
20
21
22  print(sum(one))
```

More practice!

# A Recursive `last` Algorithm Demo

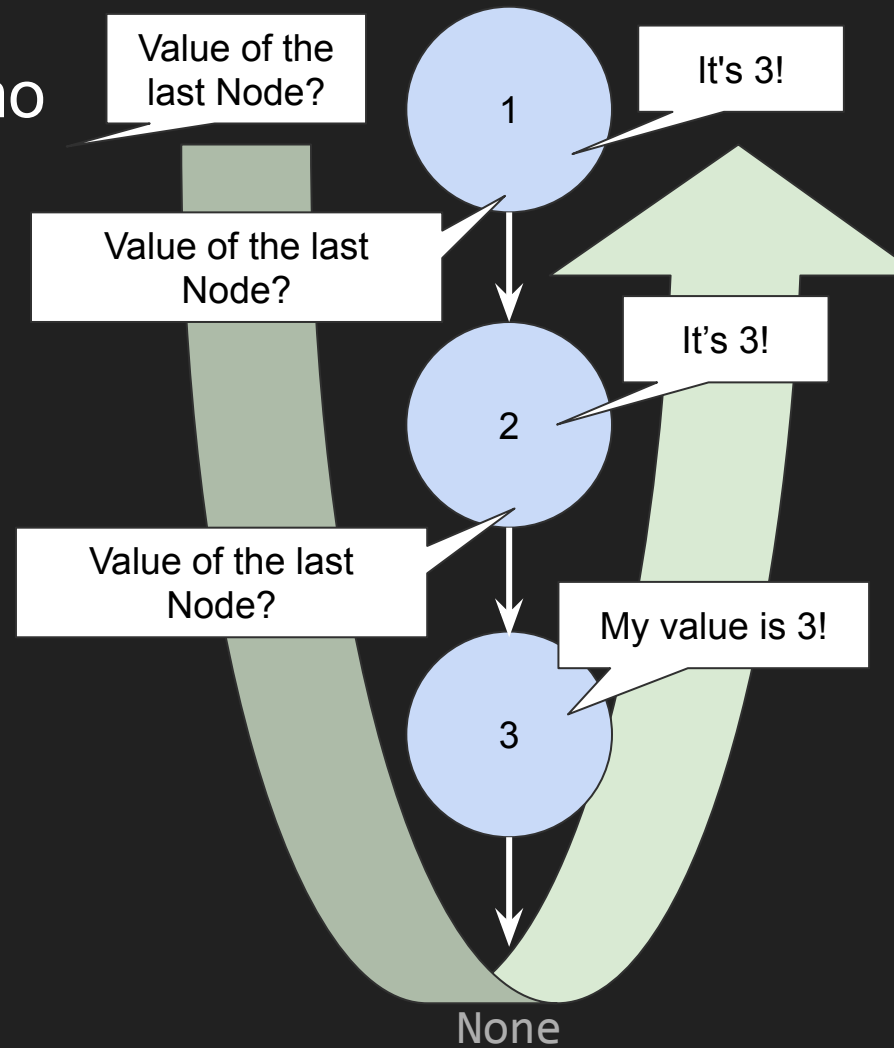
1. When you are asked,  
"What is the value of the last Node?"

If you're ***not the last Node***:

2. Ask the ***next*** Node,  
"What is the value of the last Node?"  
Wait patiently for an answer!
3. Once the answer is returned back to you,  
turn to the person who asked you and  
give them this answer.

If you ***are the last Node***:

2. Tell them, "my value is \_\_\_\_!" and share your value.





Let's write the `last` function in VS Code!



# insert\_after Algorithm Demo

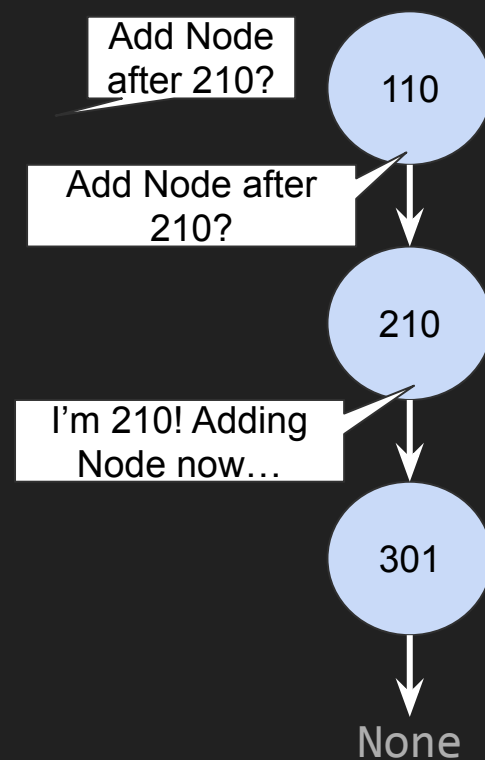
1. When you are asked,  
"Can you add a Node with a value of 211 after the  
Node with value 210?"

If your value **is not 210**:

2. Ask the **next** Node,  
"Can you add a Node with a value of 211 after the  
Node with value 210?"  
Wait patiently for an answer!
3. Once the answer is returned back to you, turn to  
the person who asked you and give them this  
answer.

If your value **is 210**:

2. Invite a new friend to the list! You will now point to  
them, and they will point to the person you were  
previously pointing to. New Node, you'll say "I was  
added!!"



# insert\_after Algorithm Demo

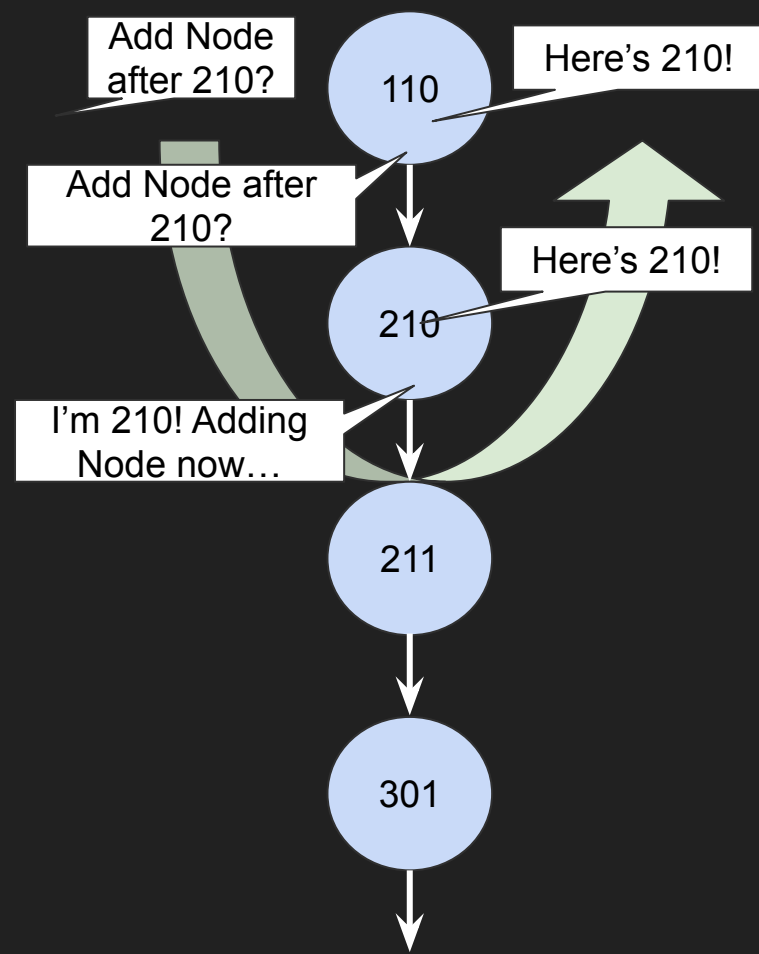
1. When you are asked,  
"Can you add a Node with a value of 211 after the  
Node with value 210?"

If your value **is not 210**:

2. Ask the next Node,  
"Can you add a Node with a value of 211 after the  
Node with value 210?"  
Wait patiently for an answer!
3. Once the answer is returned back to you, turn to  
the person who asked you and give them this  
answer.

If your value **is 210**:

2. Invite a new friend to the list! You will now point to  
them, and they will point to the person you were  
previously pointing to. New Node, you'll say "I was  
added!!"



Let's write pseudocode for the `insert_after` function

Let's write the `insert_after` function in VS Code!  